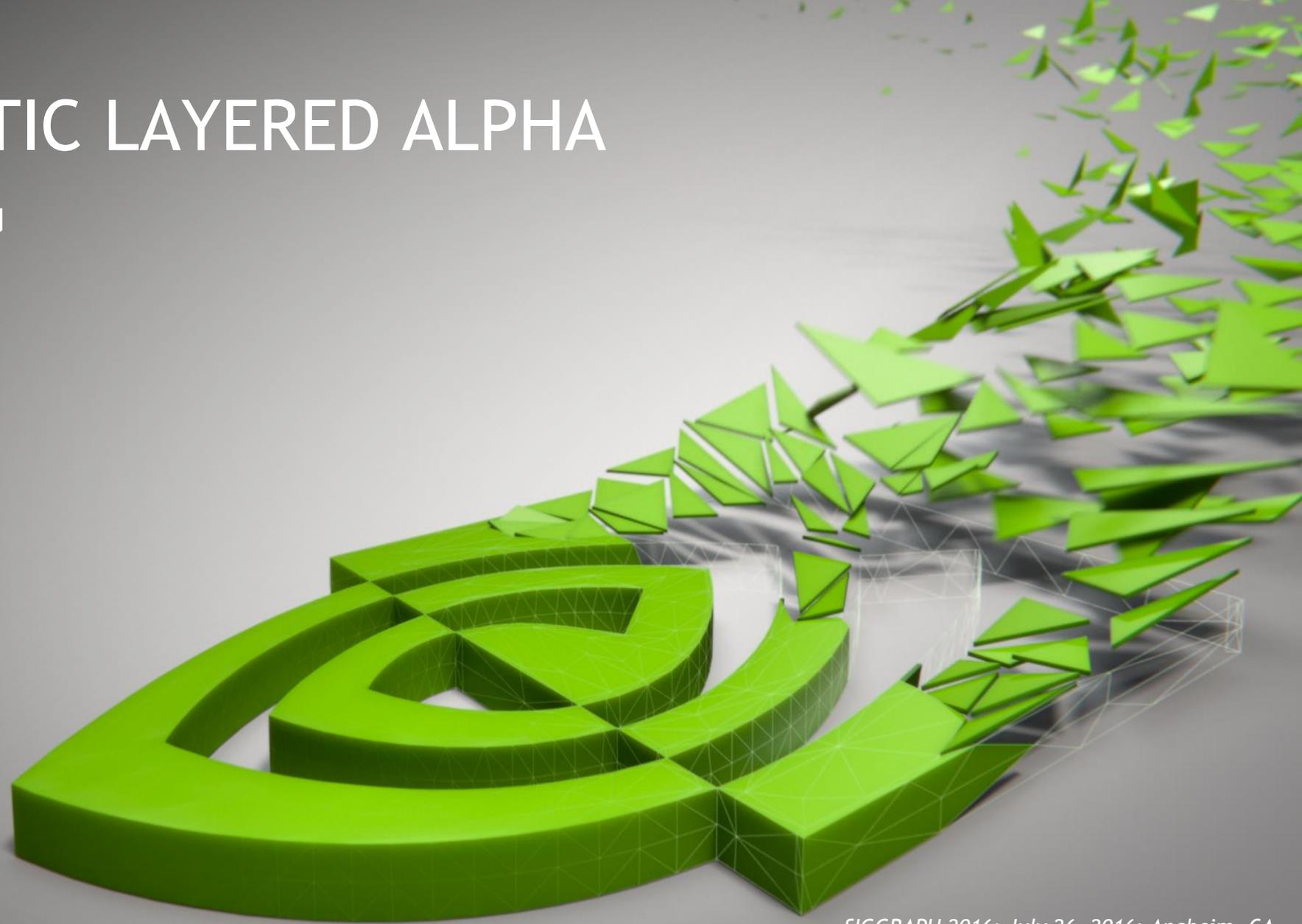


STOCHASTIC LAYERED ALPHA BLENDING

Chris Wyman



TRANSPARENCY IS HARD

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 - ▶ In real time, transparency is hard



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 - ▶ Not in same rendering pass as opaque
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 - ▶ (Some) greedily use memory
 - ▶ Often use complex locking and atomics



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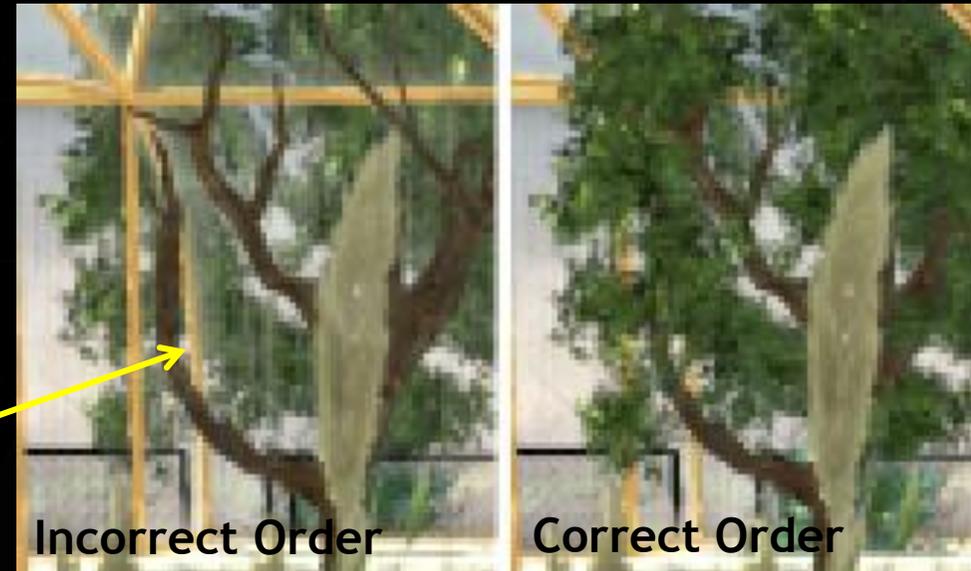
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 - ▶ Often use complex locking and atomics
- ▶ Takeaway:
 - ▶ Current solutions not ideal; many minimize use of transparency



WHAT'S THE PROBLEM?

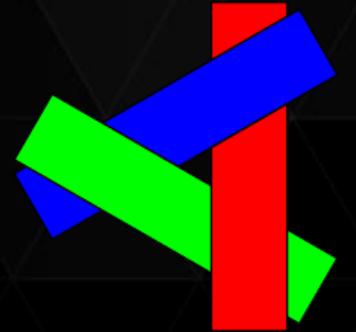
- ▶ [Porter and Duff 84] outlined numerous common compositing operations
 - ▶ The “over” operator, using multiplicative blending, describes most real interactions:
$$c_{result} = \alpha_0 c_0 + (1 - \alpha_0) \alpha_1 c_1$$
 - ▶ For streaming compute, you need to sort geometry or keep all α_i and c_i around

Merge two fragments then later try to insert one in between?



WHAT'S THE PROBLEM?

- ▶ Sorting geometry in advance can fail
 - ▶ May be no “correct” order for triangles
- ▶ Keep a list of fragments per pixel (i.e., A-Buffers [Carpenter 84])
 - ▶ Virtually unbounded** GPU memory
 - ▶ Still need to sort fragments to apply over operator in correctly
- ▶ Not just a raster problem; affects ray tracing, too
 - ▶ Unless it guarantees ray hits returned perfectly ordered



RECENT WORK: OIT CONTINUUM

* See my High Performance Graphics 2016 paper

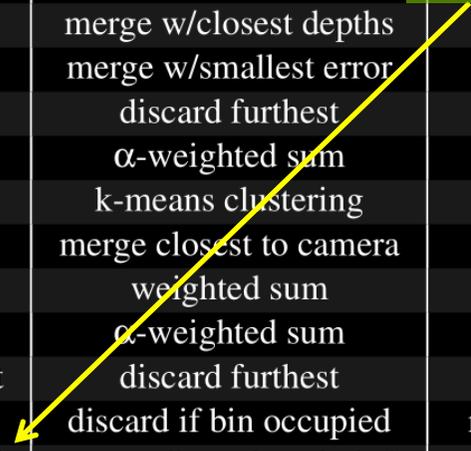
Algorithm	Memory Limit	Insertion Heuristic	Merge Heuristic	Normalize?	Use Alpha or Coverage?
A-buffer [Car84]	none	always	no merging	no	either [†]
Alpha Testing	1 layer	if $\alpha >$ thresh	discard furthest	no	alpha
Alpha Compositing [PD84]	1 layer	always	<i>over</i> operator	no	alpha
Screen-Door Transparency [FGH*85]	k z-samples	always	z-test, discard occluded	no	coverage
Z ³ [JC99]	k layers	always	merge w/closest depths	no	alpha
Deep Shadow Maps [LV00]	k line segments	always	merge w/smallest error	no	alpha
Depth Peeling [Eve01]	1 layer	if closest	discard furthest	no	either [†]
Opacity Shadow Maps [KN01]	k bins	always	α -weighted sum	no	alpha
Density Clustering [MKBVR04]	k bins	always	k-means clustering	no	alpha
k-Buffers [BCL*07]	k layers	always	merge closest to camera	no	alpha
Sort-Independent Alpha Blending [Mes07]	1 layer	always	weighted sum	no	alpha
Deep Opacity Maps [YK08]	k bins	always	α -weighted sum	no	alpha
Multi-Layer Depth Peeling [LHLW09]	k layers	if in k closest	discard furthest	no	either [†]
Occupancy Maps [SA09]	k bins	always	discard if bin occupied	renormalize alpha	alpha
Stochastic Transparency [ESSL10]	k samples	stochastic	z-test, discard occluded	α -weighted average	coverage
Fourier Opacity Maps [JB10]	k Fourier coefs	always	sum in Fourier domain	no	alpha
Adaptive Volumetric Shadow Maps [SVLL10]	k layers	always	merge w/smallest error	no	alpha
Transmittance Function Maps [DGMF11]	k DCT coefs	always	sum in DCT basis	no	alpha
Adaptive Transparency [SML11]	k layers	always	merge w/smallest error	no	alpha
Hybrid Transparency [MCTB13]	k layers	always	discard furthest	α -weighted average	alpha
Weighted Blended OIT [MB13]	empirical func	never	discard all	α -weighted average	alpha
Multi-Layer Alpha Blending [SV14]	k layers	always	merge furthest	no	alpha
Phenomenological OIT [MM16]	empirical func	never	discard all	α -weighted average	alpha

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Interesting note



**So what is
Stochastic Layered Alpha Blending?**

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WHAT IS STOCHASTIC LAYERED ALPHA BLEND

- ▶ Shows how to use *stochasm* in a k -buffer algorithm
 - ▶ I.e., allows stochastic insertion of fragments
- ▶ Shows stochastic transparency $\equiv k$ -buffering
- ▶ How?
 - ▶ By providing an explicit parameter that transitions
 - ▶ Stochastic transparency [Enderton 10] \leftrightarrow hybrid transparency [Maule 13]



**To Understand:
Start With Stochastic Transparency**

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 - ▶ *(MSAA pattern simplified for display)*

Values represent current depth sample

1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0
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0.5	1.0	1.0	0.5
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0.5	1.0	0.7	0.5
0.7	0.5	0.5	0.7
0.5	0.7	0.5	0.5
1.0	0.5	0.7	1.0

Set 8 samples to blue; depth test each

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Values represent current depth sample

0.5	0.3	0.7	0.3
0.7	0.5	0.5	0.3
0.5	0.3	0.3	0.5
0.3	0.3	0.7	0.3

Set 8 samples to green; depth test each

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Values represent current depth sample

0.5	0.3	0.7	0.3
0.7	0.5	0.5	0.3
0.5	0.3	0.3	0.5
0.3	0.3	0.7	0.3

Set 16 samples to yellow; depth test each

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 - ▶ Fourth: draw yellow fragment, $z = 0.9$, $\alpha = 1.0$
- ▶ 2nd pass accum. color using this as depth oracle

Values represent current depth sample

0.5	0.3	0.7	0.3
0.7	0.5	0.5	0.3
0.5	0.3	0.3	0.5
0.3	0.3	0.7	0.3

OBSERVATIONS

- ▶ Can lose surfaces (like yellow one)
 - ▶ But it still converges; surface loss is *stochastic*

0.5	0.3	0.7	0.3
0.7	0.5	0.5	0.3
0.5	0.3	0.3	0.5
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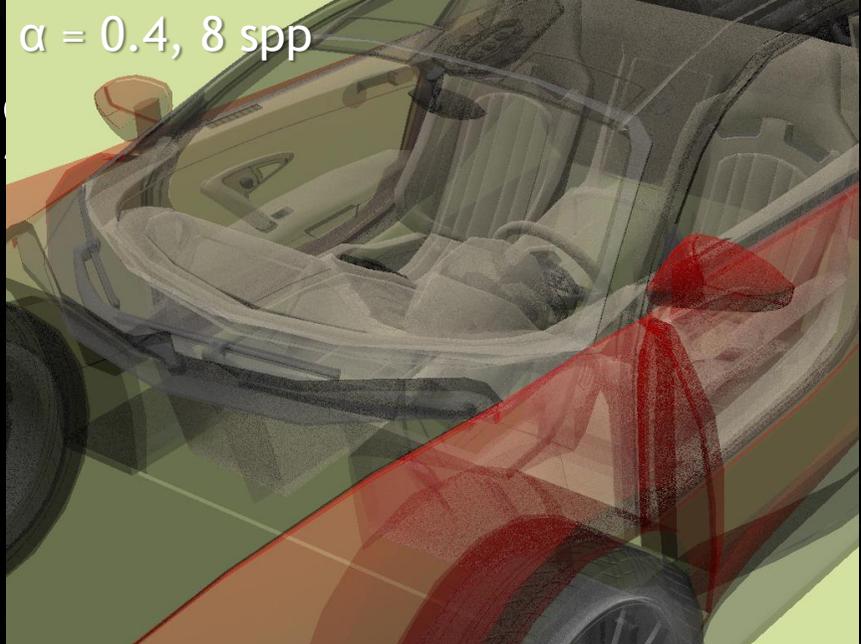
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- ▶ Can lose surfaces (like yellow one)
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- ▶ Loss worse if nearby surfaces almost opaque
 - ▶ Could easily lose blue surface

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0.5	0.3	0.3	0.5
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 - ▶ Dashboard and seat noisier with high alpha than low!



Note: Even uses stratified sampling!

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- ▶ Seems wasteful to store 8 copies of $z = 0.3$ **
 - ▶ Why not store one copy of $z = 0.3$ and a coverage mask?

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0.5	0.3	0.3	0.5
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- ▶ Seems wasteful to store 8 copies of $z = 0.3$ **
 - ▶ Why not store one copy of $z = 0.3$ and a coverage mask?
- ▶ *Implicitly* layered – stores (up to) 16 surfaces per pixel (for 16x MSA)
 - ▶ Also wasteful to store just 3 layers in a structure that can hold 16

0.5	0.3	0.7	0.3
0.7	0.5	0.5	0.3
0.5	0.3	0.3	0.5
0.3	0.3	0.7	0.3

Stochastic Layered Alpha Blending (SLAB)

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 - ▶ Merging: if $> k$ layers, simply discard the furthest
- ▶ Identical results to k spp stoc. transparency, if $k \geq b$
 - ▶ But can independently change values of k and b
 - ▶ Useful since stoc. transp. rarely stores k surfaces in a k -sample buffer
 - ▶ Also can explicitly increase b much further \rightarrow reduce noise on existing layers

WHAT IS STOCHASTIC LAYERED ALPHA BLEND?

- ▶ Our same example from before:
 - ▶ First: draw red fragment, $z = 0.5$, $\alpha = 0.5$



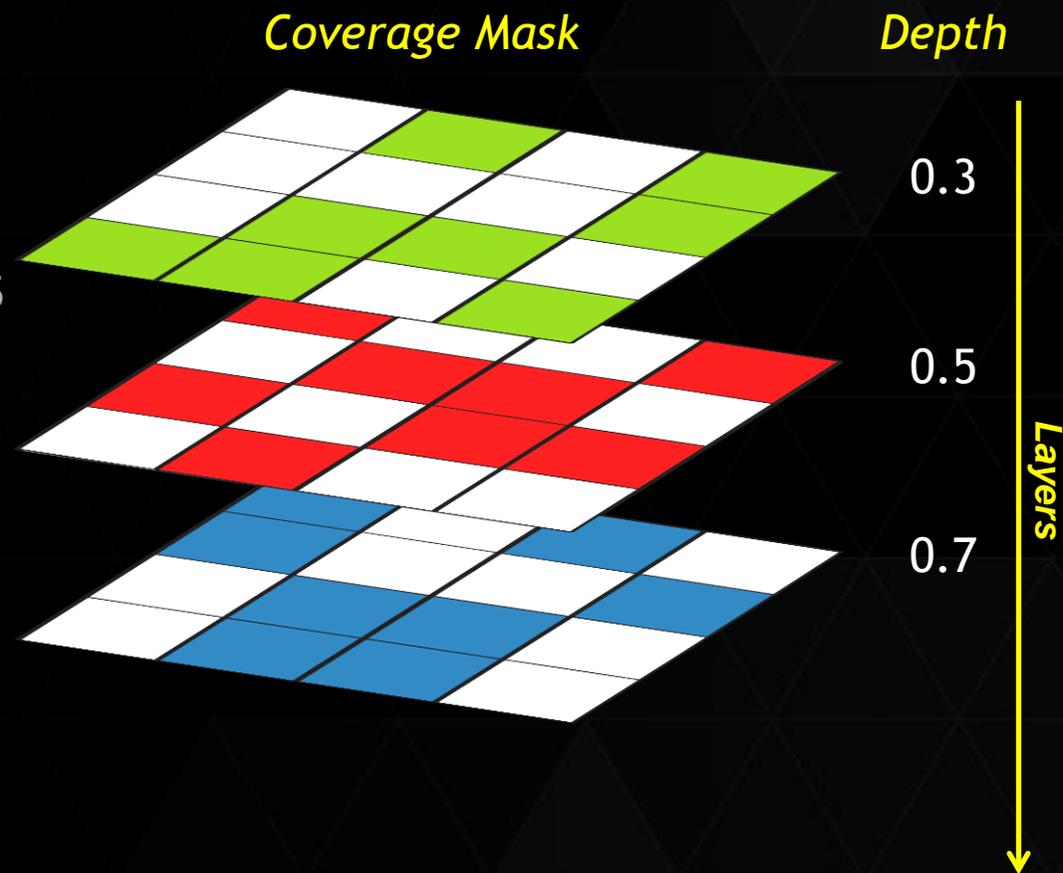
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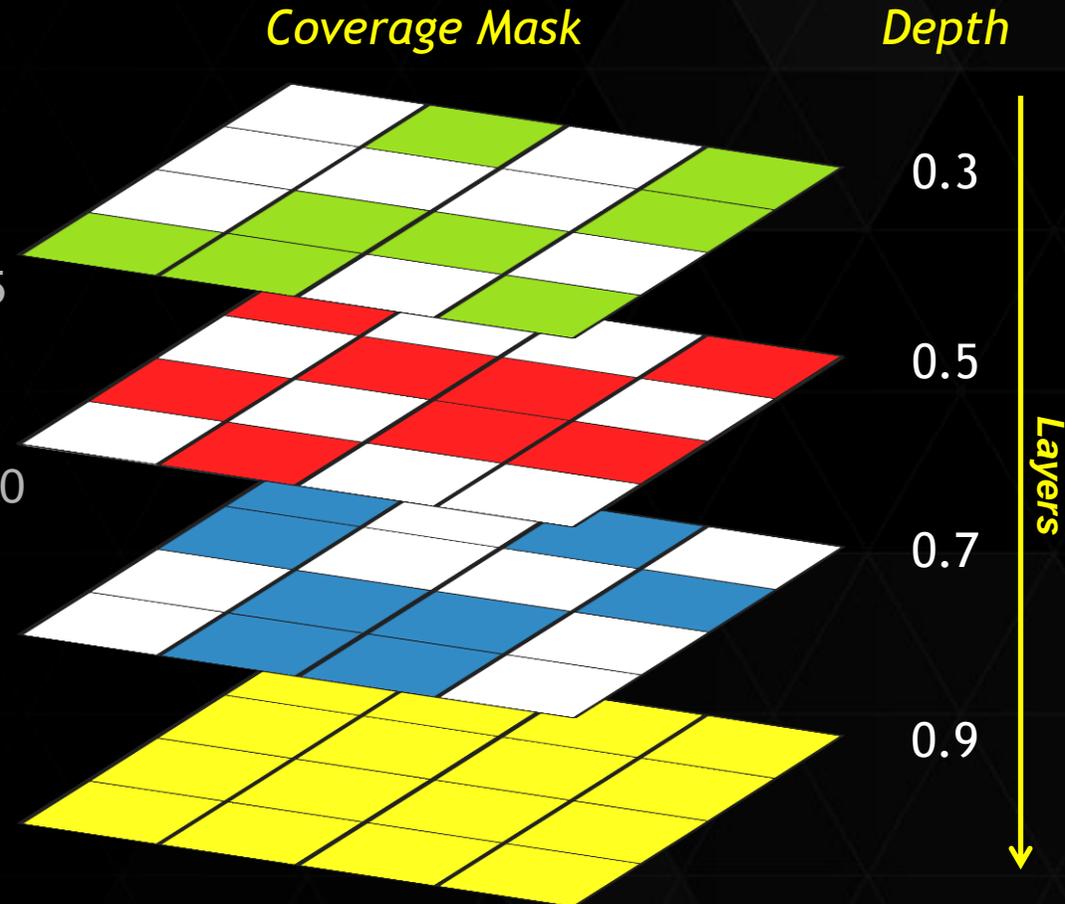
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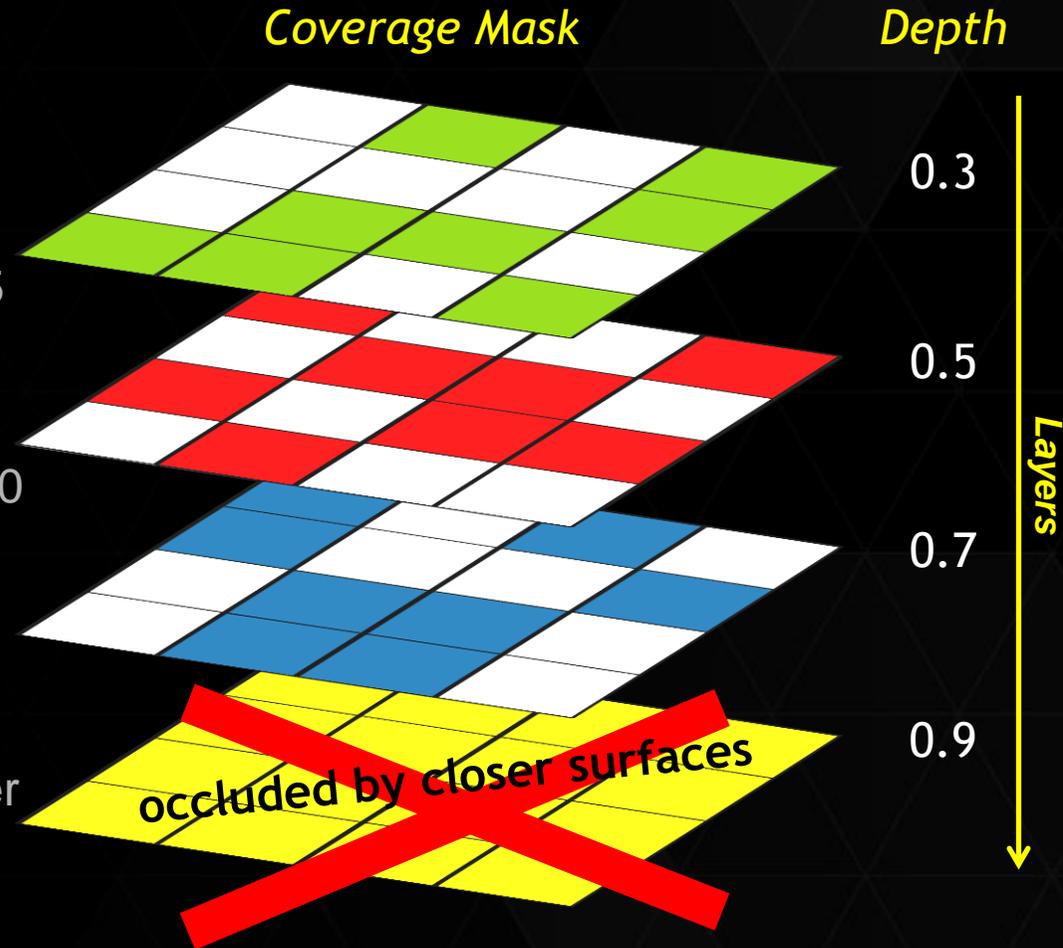
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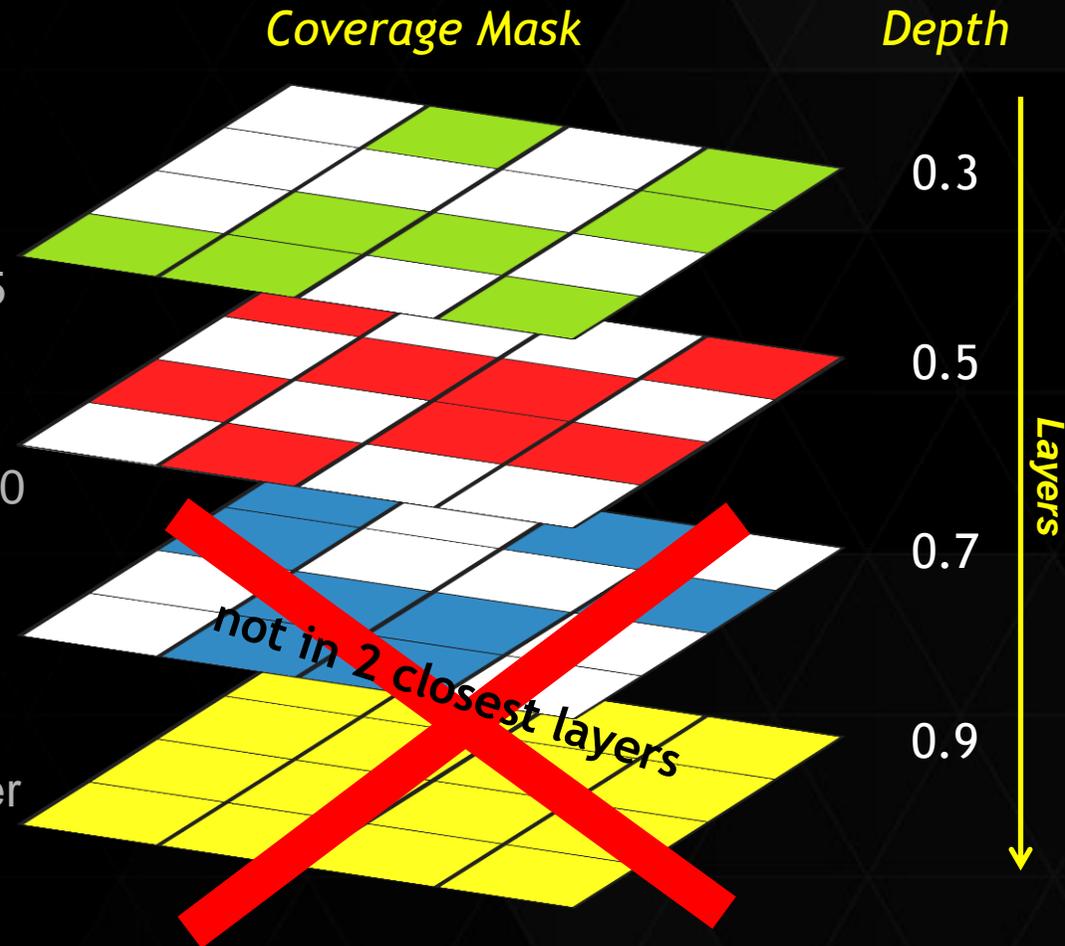
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- ▶ Layers get inserted only if not occluded
 - ▶ Adds stochasm, if masks randomly chosen
 - ▶ Different random masks might keep this layer



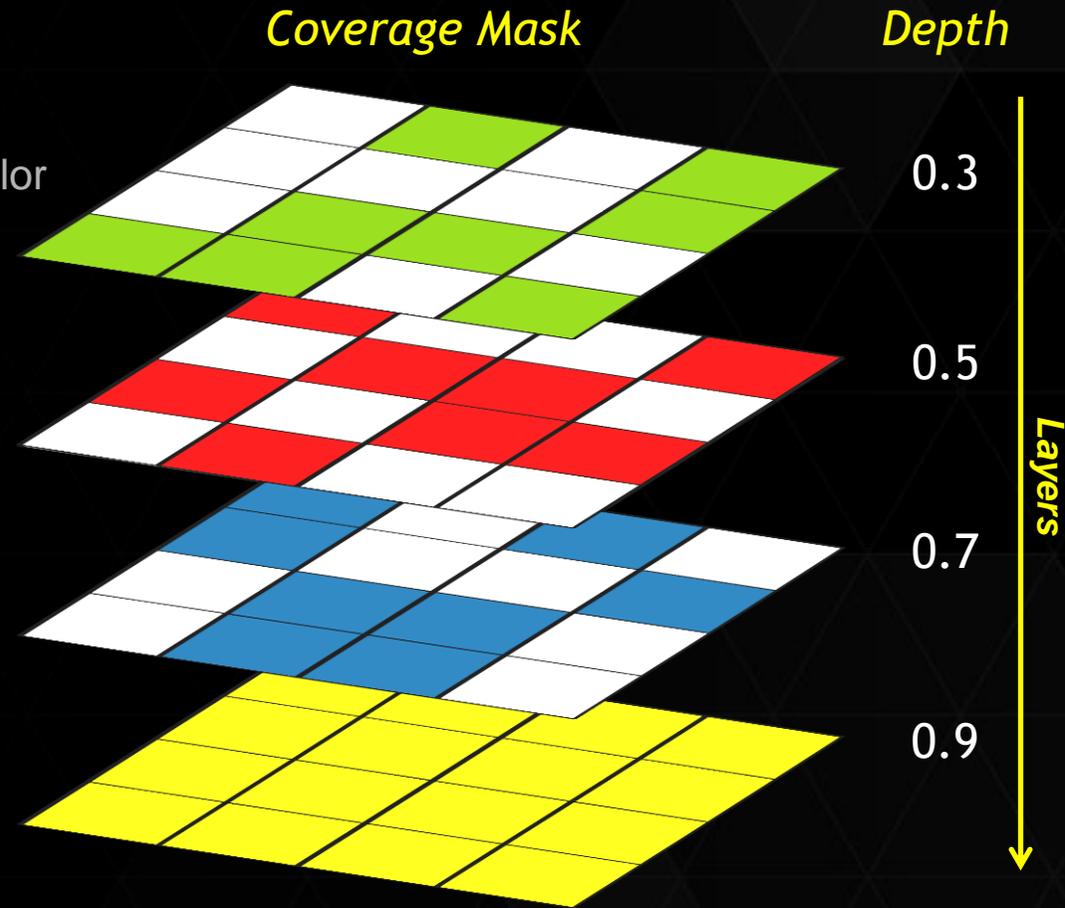
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- ▶ If $k = 2$, layers beyond 2nd get discarded



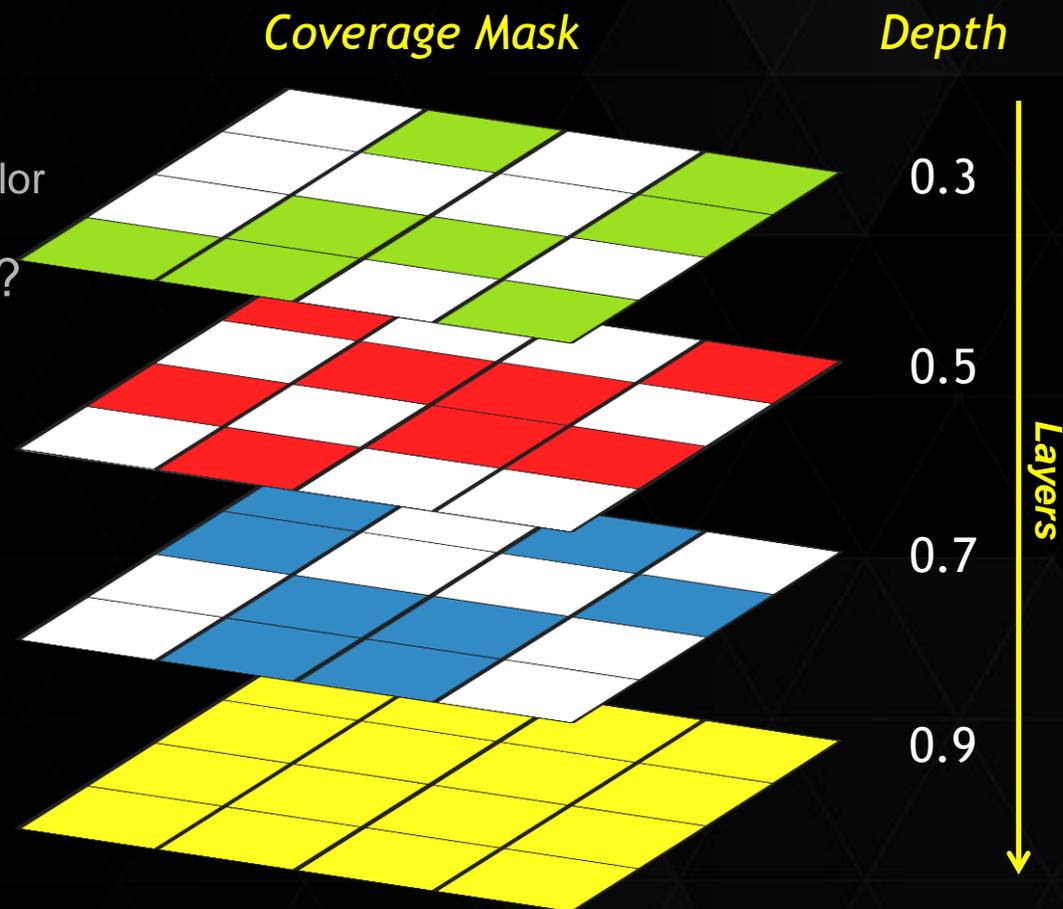
ADJUSTING PARAMETERS

- ▶ Aim to reduce noise
 - ▶ One way: avoid discarding layers that impact color



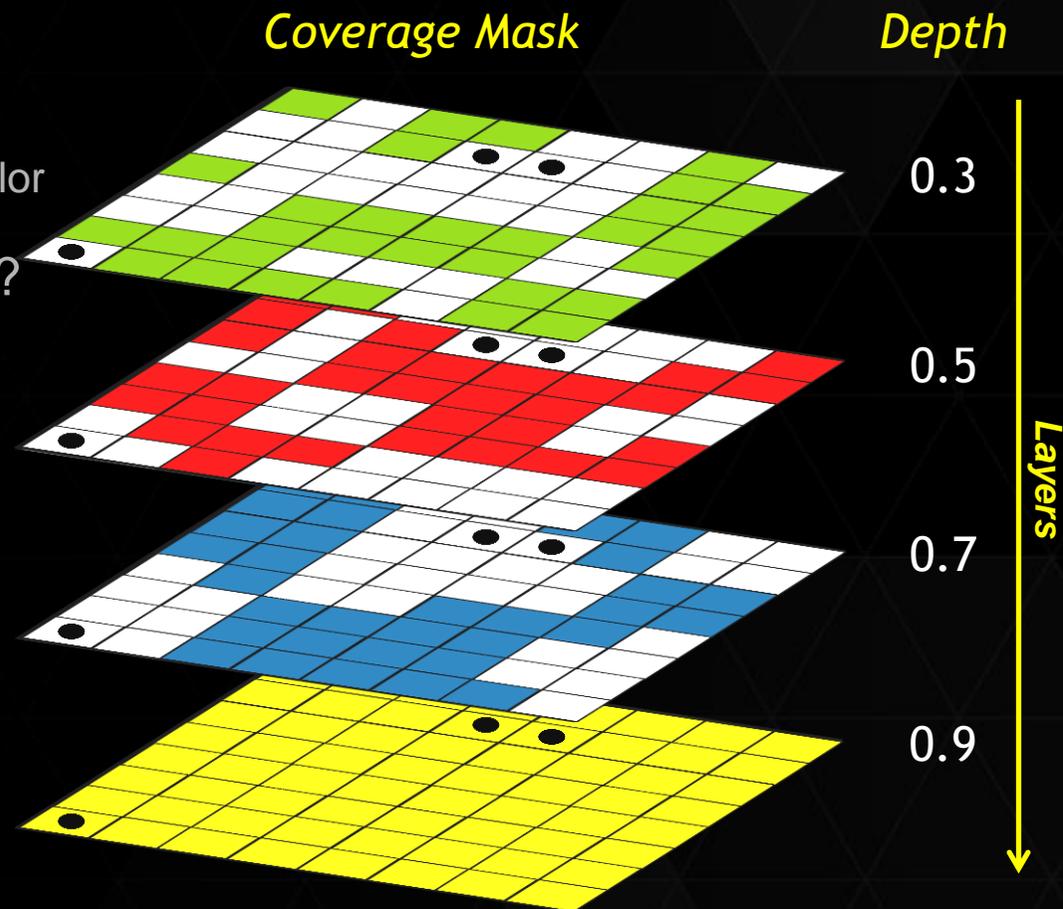
ADJUSTING PARAMETERS

- ▶ Aim to reduce noise
 - ▶ One way: avoid discarding layers that impact color
- ▶ How to increase chance to store yellow frag?



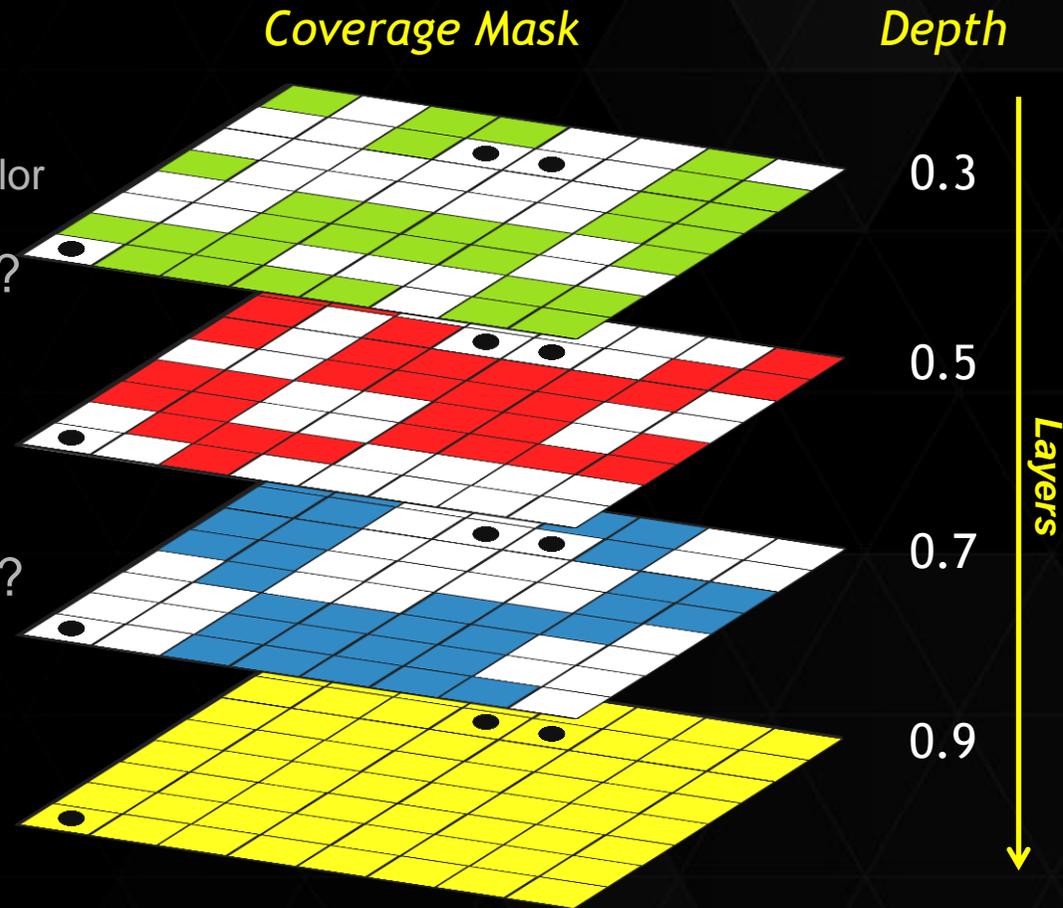
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- ▶ Aim to reduce noise
 - ▶ One way: avoid discarding layers that impact color
- ▶ How to increase chance to store yellow frag?
 - ▶ Increase number of bits in coverage mask



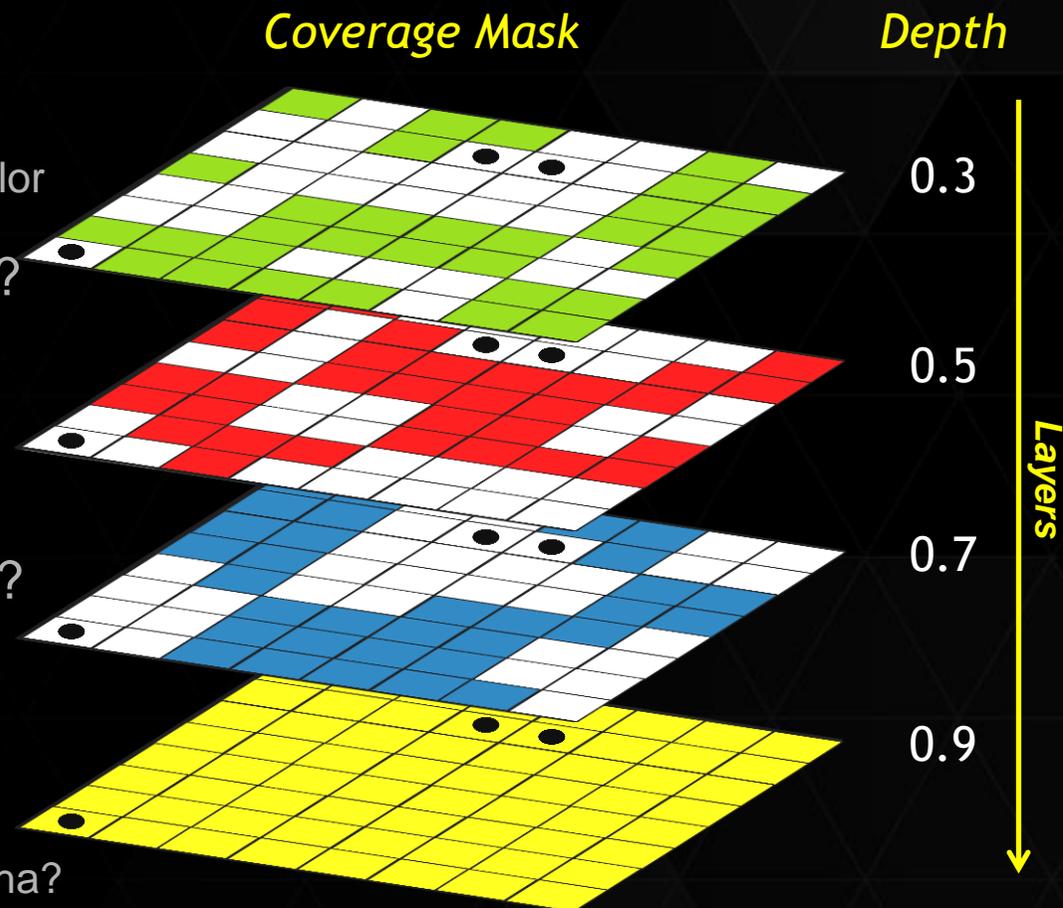
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 - ▶ Increase number of bits in coverage mask
- ▶ Larger coverage masks → lower noise
- ▶ What happens as # coverage bits increases?



ADJUSTING PARAMETERS

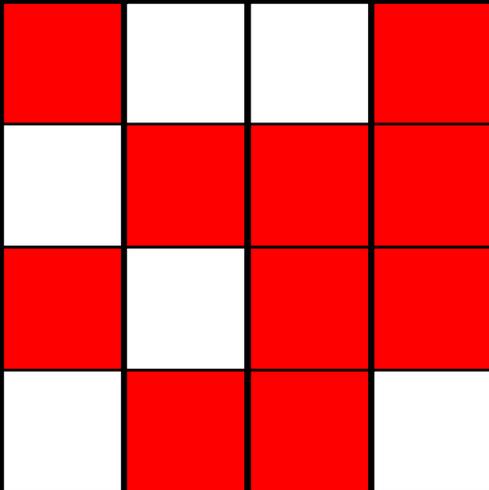
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 - ▶ One way: avoid discarding layers that impact color
- ▶ How to increase chance to store yellow frag?
 - ▶ Increase number of bits in coverage mask
- ▶ Larger coverage masks → lower noise
- ▶ What happens as # coverage bits increases?
 - ▶ Starts to behave as alpha
- ▶ Interesting to ask:
 - ▶ Can we stochastically insert fragments using alpha?



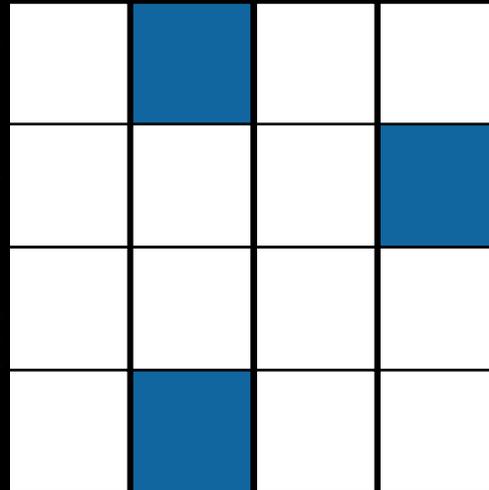
SLAB USING IMPLICIT COVERAGE

- ▶ Let's compute an insertion probability
 - ▶ Q: What's the chance random bitmask B is visible behind random bitmask A?

Bitmask A

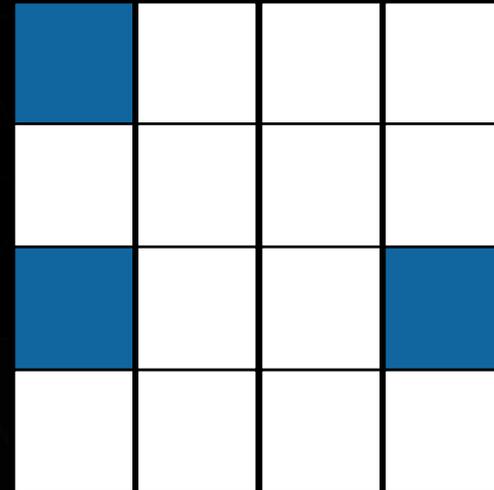


Bitmask B₀



Visible 

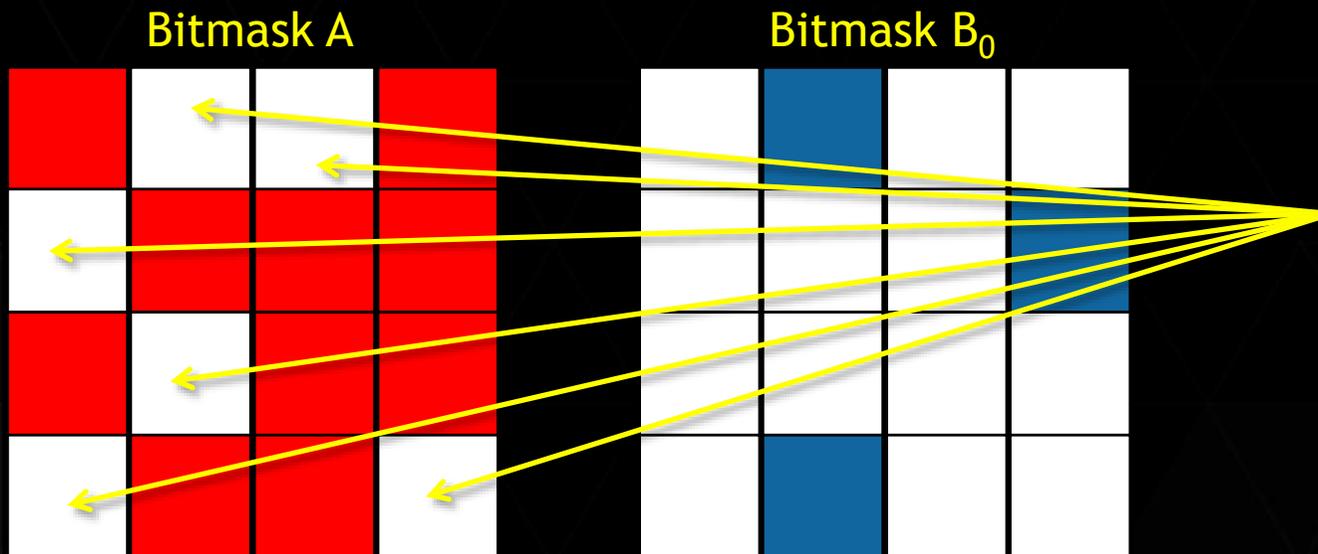
Bitmask B₁



Hidden 

SLAB USING IMPLICIT COVERAGE

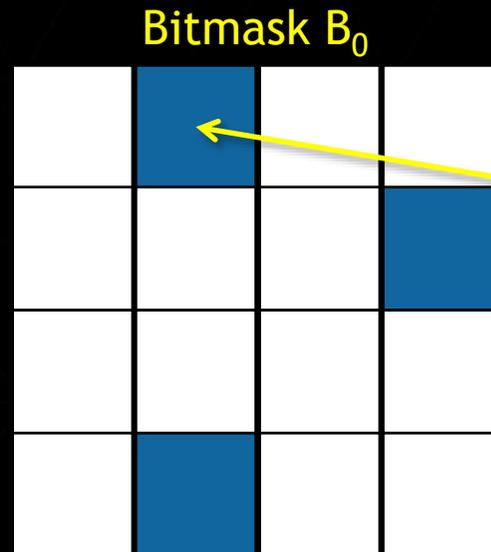
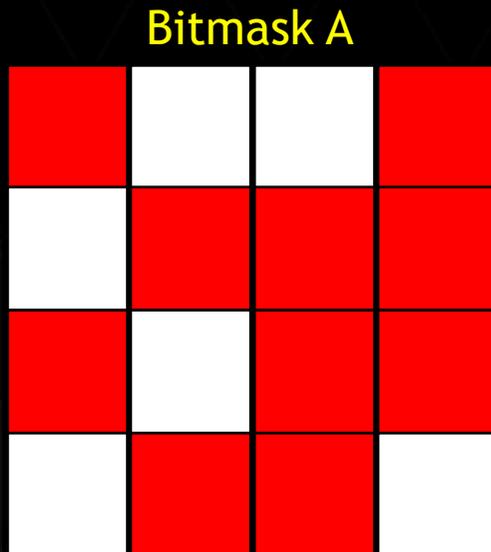
- ▶ Let's compute an insertion probability
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Hidden if *none* of these get covered by bits in bitmask B

SLAB USING IMPLICIT COVERAGE

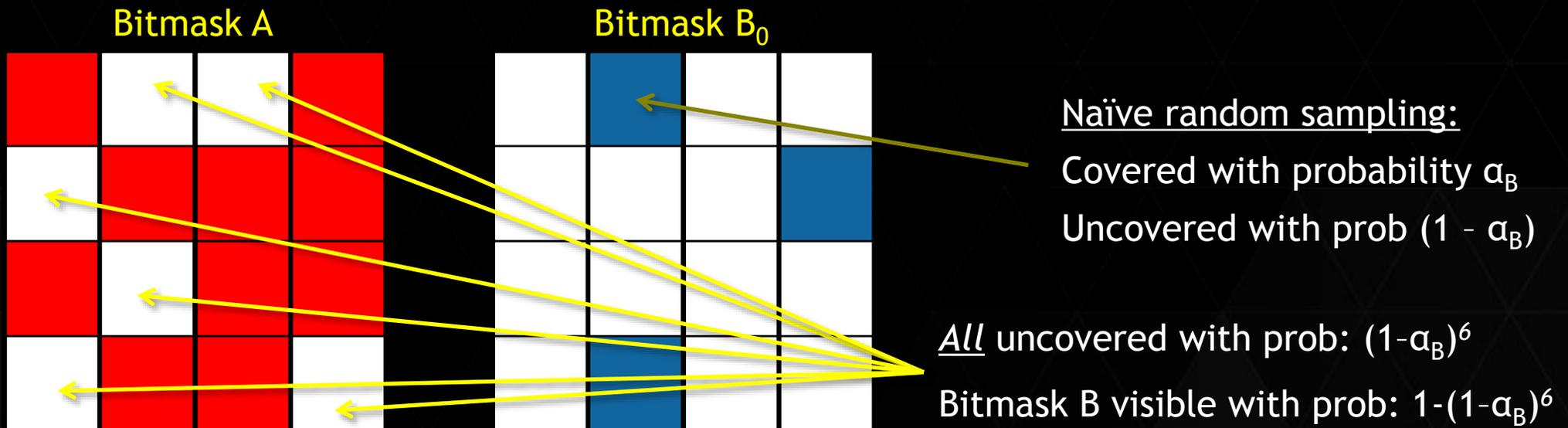
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Naïve random sampling:
Covered with probability α_B
Uncovered with prob $(1 - \alpha_B)$

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SLAB USING IMPLICIT COVERAGE

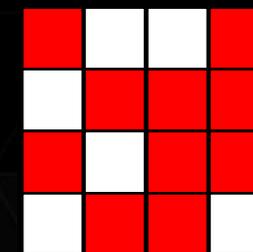
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$$P_b(\beta_A, \beta_B) = 1 - \left(1 - \frac{\beta_B}{b}\right)^{(b - \beta_A)}$$

Or

$$P_b(\beta_A, \alpha_B) = 1 - (1 - \alpha_B)^{(b - \beta_A)}$$

Bitmask A



$\beta_A \equiv \#$ bits covered
 $\beta_A = \lfloor \alpha_A b \rfloor$ or $\lceil \alpha_A b \rceil$
for b bits in bitmask

SLAB USING IMPLICIT COVERAGE

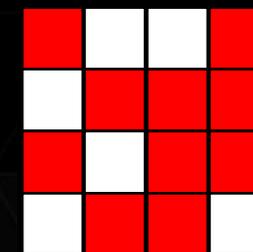
- ▶ Let's compute an insertion probability
 - ▶ Q: What's the chance random bitmask B is visible behind random bitmask A?

$$P_b(\beta_A, \beta_B) = 1 - \left(1 - \frac{\beta_B}{b}\right)^{(b - \beta_A)}$$

Or

$$P_b(\beta_A, \alpha_B) = 1 - \underbrace{\left(1 - \alpha_B\right)}_{\text{prob of leaving 1 bit uncovered}} \underbrace{\left(b - \beta_A\right)}_{\text{number of bits that must be uncovered}}$$

Bitmask A



$\beta_A \equiv \# \text{ bits covered}$
 $\beta_A = \lfloor \alpha_A b \rfloor$ or $\lceil \alpha_A b \rceil$
for b bits in bitmask

SLAB USING IMPLICIT COVERAGE

- ▶ Let's compute an insertion probability
 - ▶ Q: How about for random masks using stratified samples?

$$P_b(\beta_A, \beta_B) = \begin{cases} 1 - \frac{\beta_A!(b-\beta_B)!}{b!(\beta_A-\beta_B)!} & \text{if } \beta_B \leq \beta_A \\ 1 & \text{if } \beta_B > \beta_A \end{cases}$$



$\beta_A \equiv \#$ bits covered

- ▶ Based on combinatorics
 - ▶ Choosing dependent probabilities so all mask bits in B are covered by A

WAIT! NOT USING INFINITE # BITS?

- ▶ Both equations require a number of bits b in the coverage mask

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using stratified random samples

$$P_b(\beta_A, \beta_B) = 1 - \left(1 - \frac{\beta_B}{b}\right)^{(b-\beta_A)}$$

using naïve random samples

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- ▶ Both equations require a number of bits b in the coverage mask
 - ▶ Can ask what happens to P_b as $b \rightarrow \infty$
 - ▶ Turns out as $b \rightarrow \infty$, $P_b \rightarrow 1$
 - ▶ Instead of *stochastic* insertion of fragments, they're *always* inserted

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$$P_b(\beta_A, \beta_B) = 1 - \left(1 - \frac{\beta_B}{b}\right)^{(b-\beta_A)} \quad \text{using naïve random samples}$$

WAIT! NOT USING INFINITE # BITS?

- ▶ Both equations require a number of bits b in the coverage mask
 - ▶ Can ask what happens to P_b as $b \rightarrow \infty$
 - ▶ Turns out as $b \rightarrow \infty$, $P_b \rightarrow 1$
 - ▶ Instead of *stochastic* insertion of fragments, they're *always* inserted
- ▶ Going back to our continuum
 - ▶ When $b = k$, SLAB is equivalent to stochastic transparency
 - ▶ When $b \rightarrow \infty$, SLAB is equivalent to hybrid transparency (a variant of k-buffer)

Stochastic Transparency [ESSL10]	k samples	stochastic	z-test, discard occluded	α -weighted average	coverage
Hybrid Transparency [MCTB13]	k layers	always	discard furthest	α -weighted average	alpha
(NEW) Stochastic Layered Alpha Blending	k layers	stochastic	discard furthest	α -weighted average	either [†]

WAIT! NOT USING INFINITE # BITS?

- ▶ To get something between k-buffers and stoc. transp.
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 - ▶ Need to use $k \leq b < \infty$
 - ▶ Can do this with an *explicit* coverage mask with b random bits
 - ▶ Using deterministic insertion based on random coverage masks
 - ▶ Can do this with an *implicit* coverage (i.e., alpha) using b *virtual* bits
 - ▶ Using stochastic insertion using probability functions
 - ▶ b only controls distance along the k-buffer \leftrightarrow stoc transp continuum

Let's demonstrate

FOLIAGE MAP

(From Epic's Unreal SDK)

All surfaces $\alpha = 0.5$



FOLIAGE MAP

(From Epic's Unreal SDK)

All surfaces $\alpha = 0.5$



Stoc transp, 8 spp

SLAB, $k = b = 8$

SLAB, $k = 8, b = 32$

SLAB, $k = 8, b = 128$

SLAB, $k = 8, b = 32$
using alpha

Hybrid Transparency



FOLIAGE MAP

(From Epic's Unreal SDK)

All surfaces $\alpha = 0.5$



Stoc transp, 8 spp

SLAB, $k = b = 8$

SLAB, $k = 8, b = 32$

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SLAB, $k = 8, b = 32$
using alpha

Hybrid Transparency  NVIDIA

FOLIAGE MAP

(From Epic's Unreal SDK)

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Stoc transp, 8 spp

SLAB, $k = b = 8$

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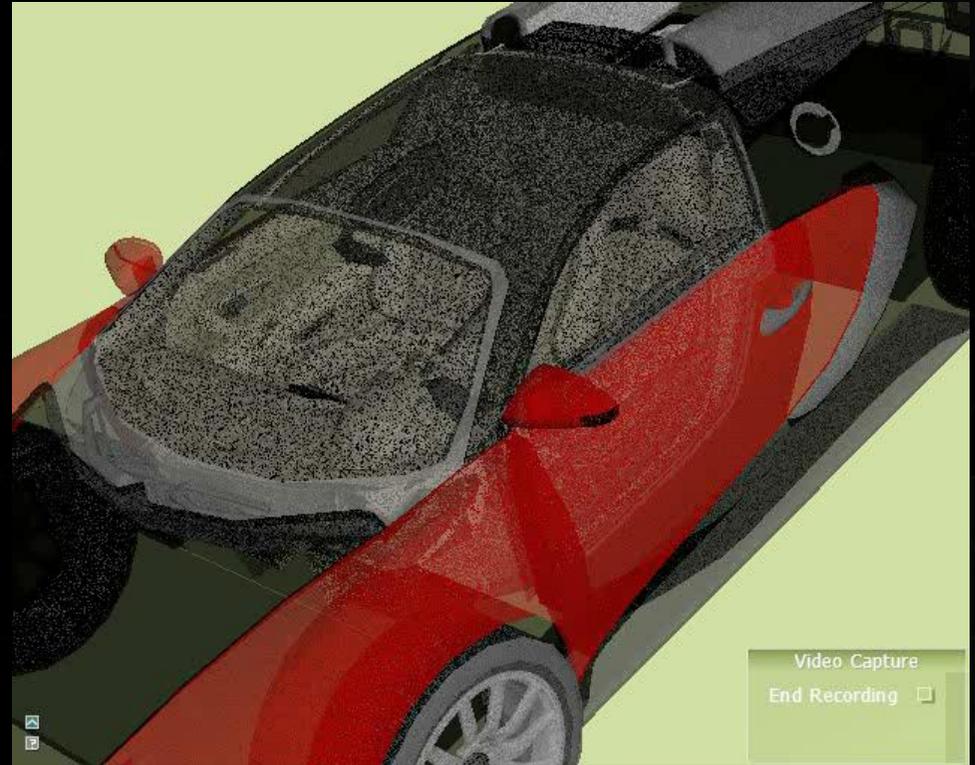
SLAB, $k = 8, b = 32$
using alpha

Hybrid Transparency  NVIDIA

STOCHASTIC TRANSPARENCY TO K-BUFFERS



Stochastic Layered Alpha Blending, $k=b=4$

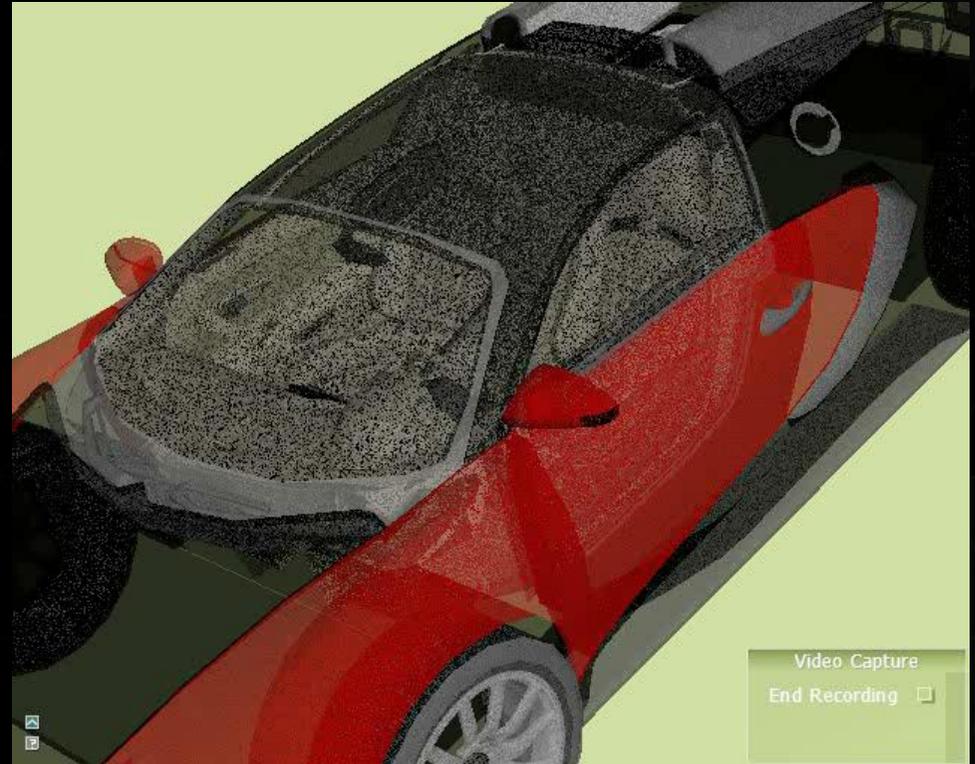


Stochastic Transparency, 4 spp

STOCHASTIC TRANSPARENCY TO K-BUFFERS



Stochastic Layered Alpha Blending, $k=4$, $b=32$

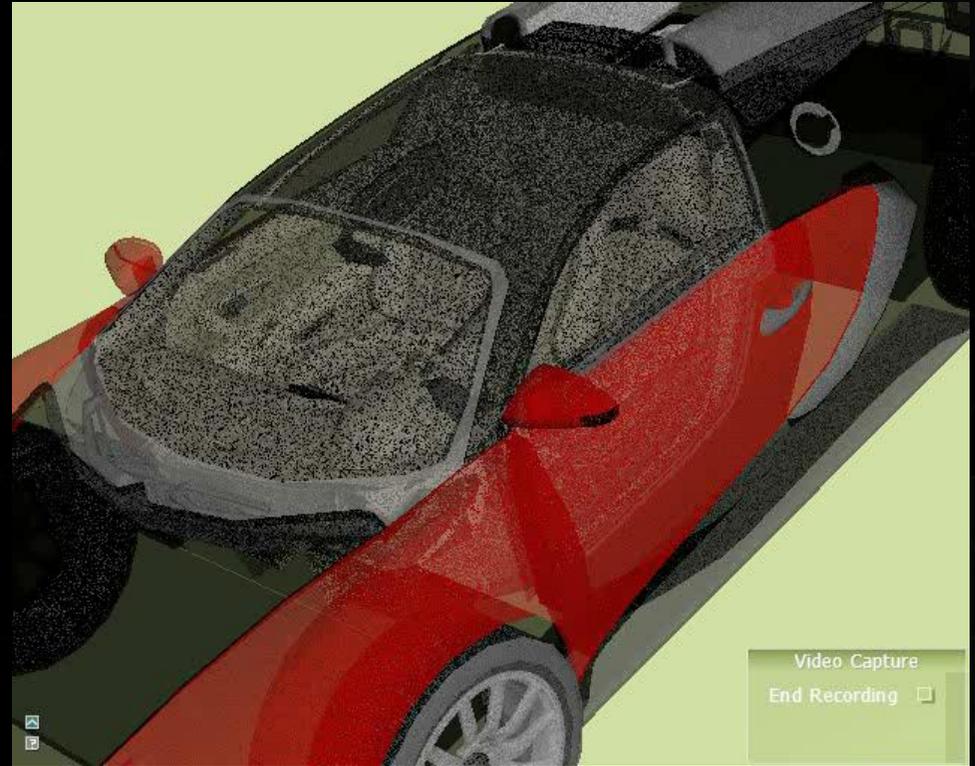


Stochastic Transparency, 4 spp

STOCHASTIC TRANSPARENCY TO K-BUFFERS



Stochastic Layered Alpha Blending, $k=4$, $b=8$
(using alpha rather than coverage)



Stochastic Transparency, 4 spp

STOCHASTIC TRANSPARENCY TO K-BUFFERS



Stochastic Layered Alpha Blending, $k=4$, $b=32$
(using alpha rather than coverage)



Hybrid Transparency, 4 layers

Summary

SUMMARY

- ▶ Proposed new algorithm
 - ▶ Stochastic layered alpha blending (SLAB)

SUMMARY

- ▶ Proposed new algorithm
 - ▶ Stochastic layered alpha blending (SLAB)
 - ▶ Key takeaways:
 - ▶ K-buffers need not be deterministic
 - ▶ Stochastic transparency and k-buffering are similar; transition via bit count
 - ▶ “Stochastic” need not mean random bitmask generation
 - ▶ Algorithms connecting others useful; here, allow trading noise for bias
 - ▶ SLAB with alpha values can stratify samples in z (between layers)
 - (Not really discussed in this talk)

QUESTIONS?

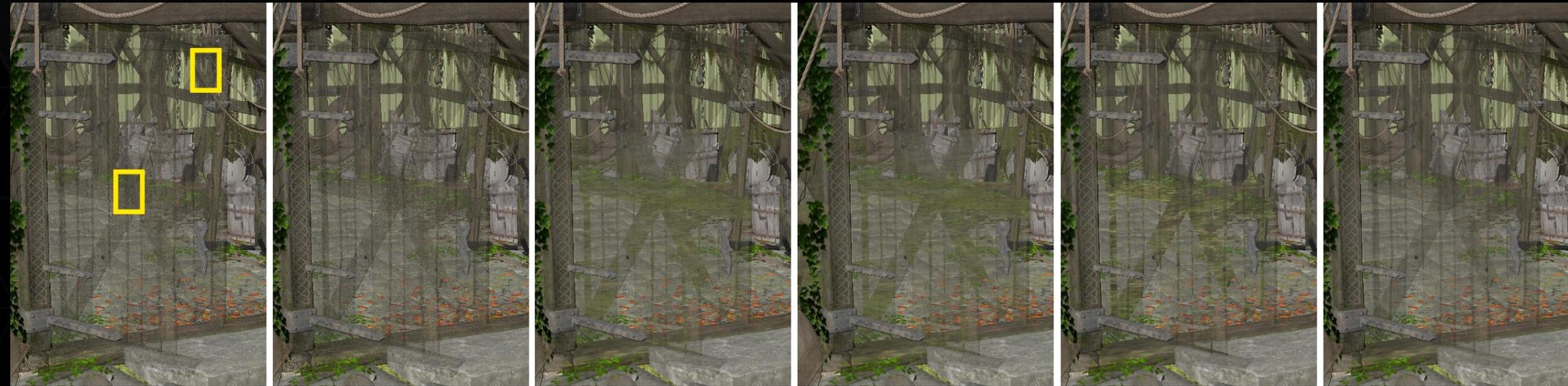
E-mail: cwyman@nvidia.com

Twitter: [@_cwyman_](https://twitter.com/_cwyman_)

Paper PDF:



Blacksmith building, from Unity's "The Blacksmith" demo



Stochastic
transparency
4 spp

SLAB
 $k = 4, b = 4$

SLAB
 $k = 4, b = 16$
using alpha

Hybrid
transparency
4 layers

Multi-layer
alpha blending
4 layers

Ground truth
(A-buffer)